



On the Singularity-free Workspace of Parallel Robots Using Interval Analysis

mmmmmmmm Hadi Farzaneh Kaloorazi¹

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Co-supervisor: Dr. Stéphan Caro²

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University of Tehran

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Outline

- 1 Parallel Robots
 - Introduction
 - Kinematics and Jacobian Analysis
- 2 Necessity of the Research
- 3 Optimization
- 4 History of the Research
 - Publications
- 5 Methodology
 - Interval Analysis
- 6 Obtained Results
 - Maximal Singularity-free Circle
- 7 Ongoing Works
- 8 Schedule
- 9 Acknowledgement

Outline

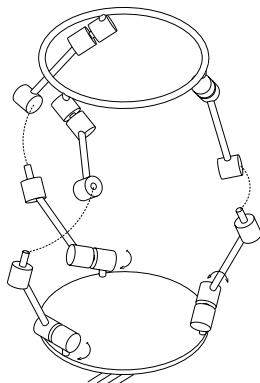
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Parallel Robots

Mechanisms under study

- Parallel mechanisms (PM)
 - Planar mechanisms
 - 6-Degree-of-freedom
 - Cable driven robots

Figure presented in a thesis by
Xianwen Kong



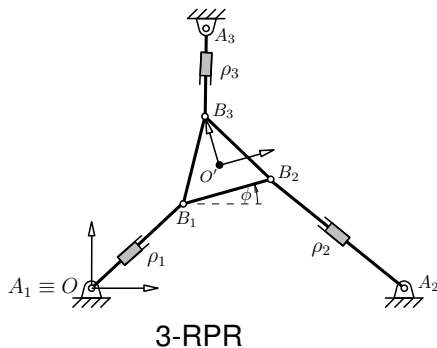
General parallel mechanism

Parallel Robots

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Figure presented in a paper by Ilian Bonev

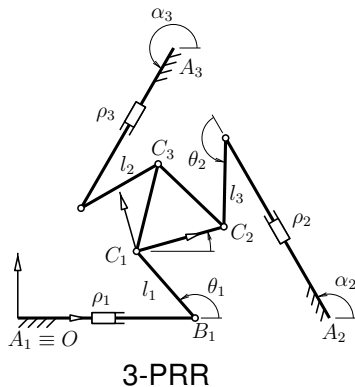


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Mechanisms under study

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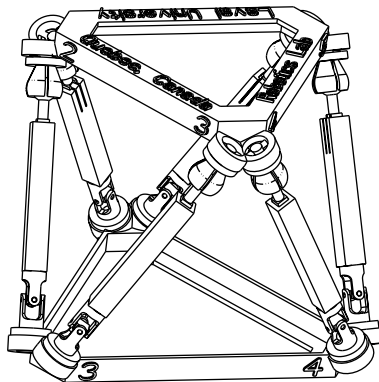


Parallel Robots

Mechanisms under study

- Parallel mechanisms (PM)
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 - 6-Degree-of-freedom
 - Cable driven robots

Built in Laval University



Gough-Stewart Platform
(MSSM)

Parallel Robots

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A Cable-driven robot, Arecibo Observatory in Puerto Rico

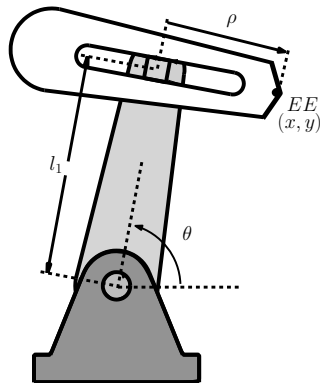
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Kinematics and Jacobian Analysis

Two kinematic properties

- **Workspace**
(Stroke of the actuators)
 - Serial manipulator
2-DoF RP (joint work)
 - 3-RPR, using interval analysis
- Singularity loci
 - 3-RPR, quadratic equations
 - 3-PRR

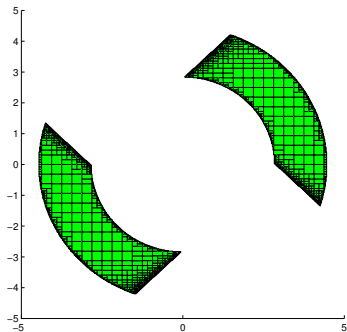


2-DoF RP serial manipulator

Kinematics and Jacobian Analysis

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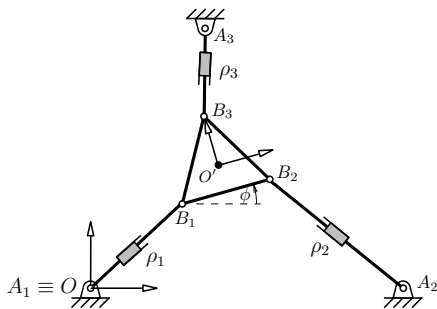


Workspace of 2-DoF RP

Kinematics and Jacobian Analysis

Two kinematic properties

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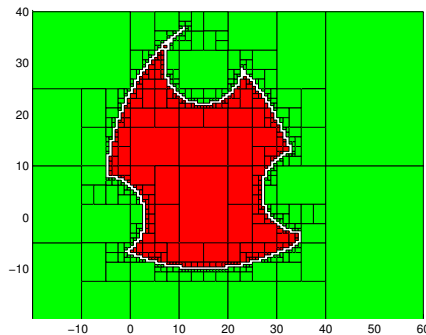


3-RPR PM

Kinematics and Jacobian Analysis

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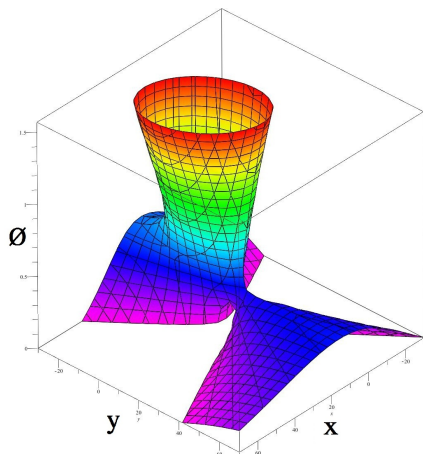


Workspace of 3-RPR PM,
implemented in Matlab

Kinematics and Jacobian Analysis

Two kinematic properties

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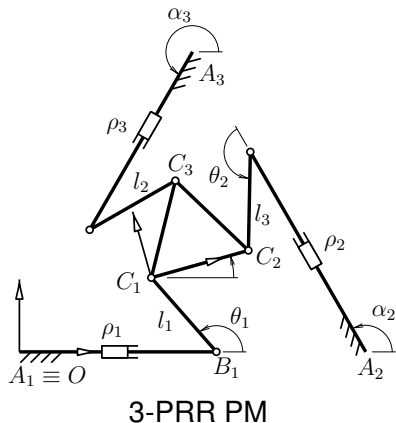


Singularity loci of 3-RPR PM

Kinematics and Jacobian Analysis

Two kinematic properties

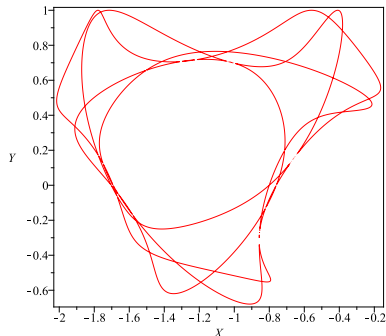
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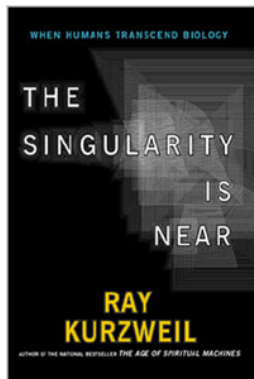


Singularity of 3-PRR PM, form implicit formulation, ezplot

Necessity of the research

Reliability

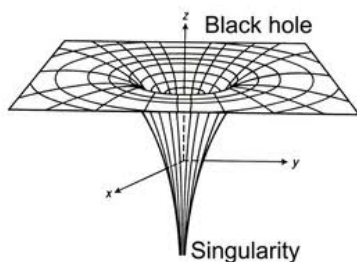
- The workspace of a mechanism must be singular-free
- Why circle?



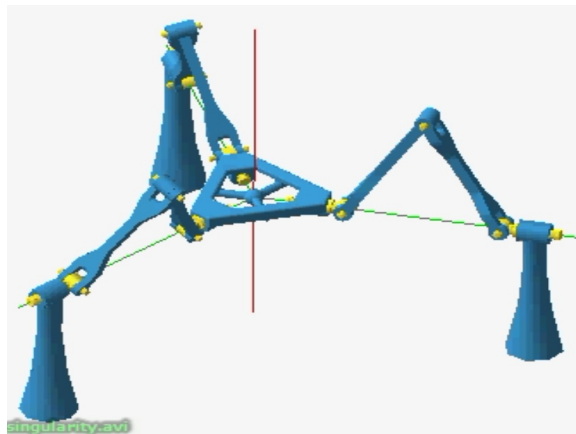
Necessity of the research

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- The workspace of a mechanism must be singular-free
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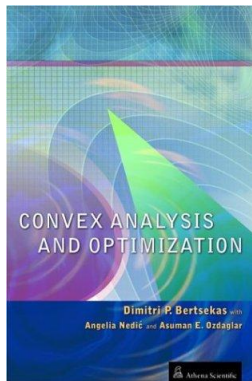
Necessity of the research



Optimization

Mathematical framework

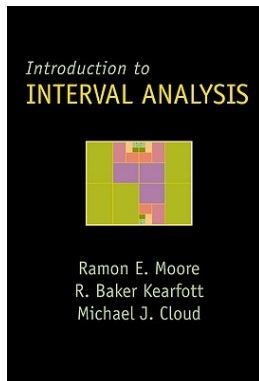
- Convex Optimization
- *Interval Analysis*
- Other methods
 - Grid (network)
 - Offset approach
 - Evolutionary approaches



Optimization

Mathematical framework

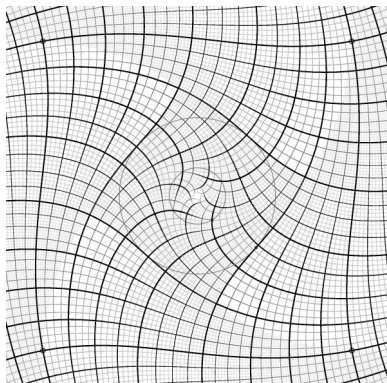
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Optimization

Mathematical framework

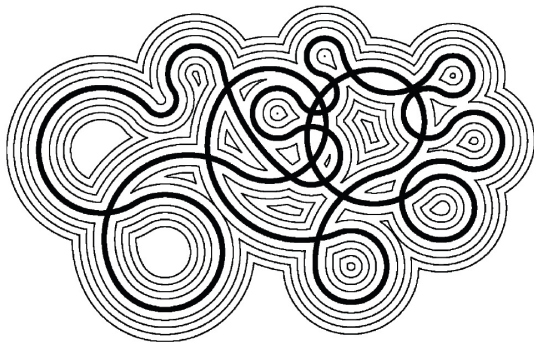
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Optimization

Mathematical framework

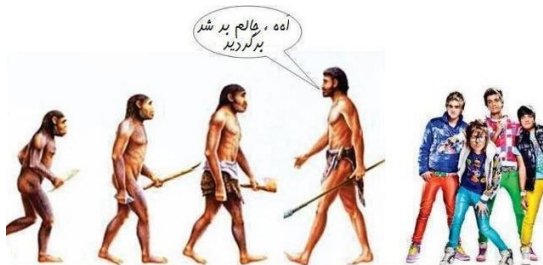
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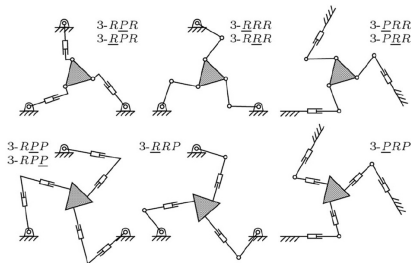
Literature

Papers

- I. Bonev, D. Zlatanov, C. Gosselin
"Singularity Analysis of 3-DOF Planar Parallel Mechanisms via Screw Theory"

Method and shortage

- Lagrangian multiplier
- Fixed center point
- Only 3-RPR



3-DoF planar parallel mechanisms

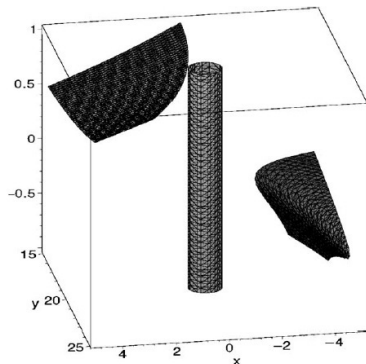
Literature

Papers

- H. Li, C. Gosselin, M. Richard "Determination of maximal singularity-free zones in the workspace of planar three-degree-of-freedom parallel mechanisms"

Method and shortage

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Maximal singularity-free cylinder with $\phi \in [-90^\circ, 90^\circ]$

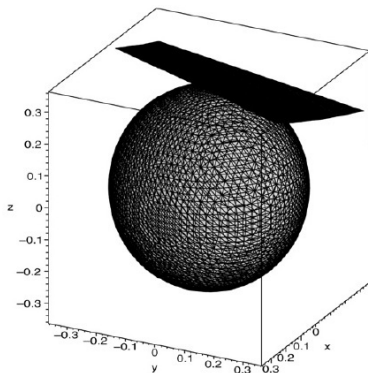
Literature

Papers

- H. Li, C. Gosselin, M. Richard "Determination of the maximal singularity-free zones in the six-dimensional workspace of the general Gough-Stewart platform"

Method and shortage

- Lagrangian multiplier
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Maximal singularity-free sphere

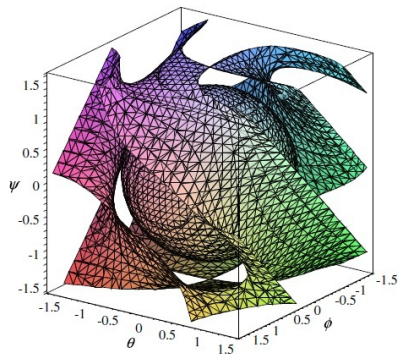
Literature

Papers

- Q. Jiang, C. Gosselin
"Determination of the maximal singularity-free orientation workspace for the Gough-Stewart platform"

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The maximal singularity sphere

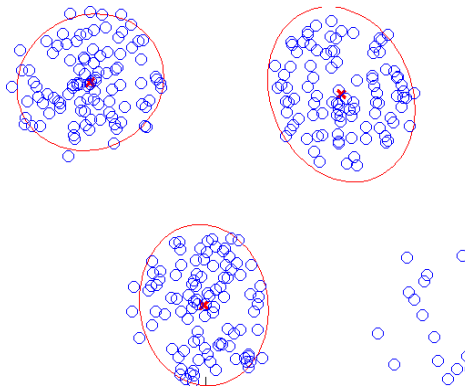
Literature

Papers

- G. Abbasnejad, H. Daniali, and S. Kazemi, "A New Approach to Determine the Maximal Singularity-free Zone of 3-RPR Planar Parallel Manipulator"

Method and shortage

- Lagrangian multiplier
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Particle Swarm Optimization
(PSO)

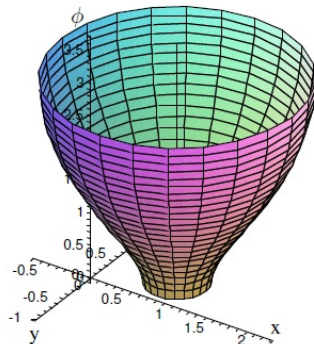
Literature

Papers

- Q. Jiang and G. C.M., "Geometric Synthesis of Planar 3-RPR Parallel Mechanisms for Singularity-free workspace"

Method and shortage

- Lagrangian multiplier
- Fixed center point
- Only 3-RPR



Evolution of the singularity circle vs ϕ

Literature

Papers

- Q. Jiang and C. Gosselin, "The Maximal Singularity-Free Workspace of Planar 3-RPR Parallel Mechanisms"

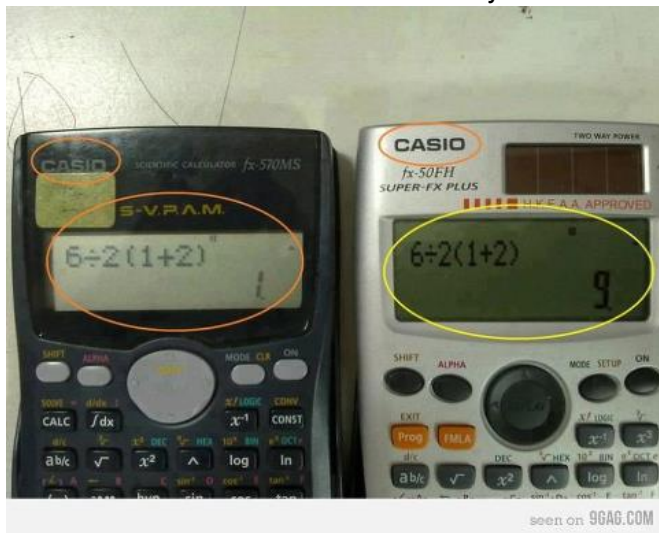
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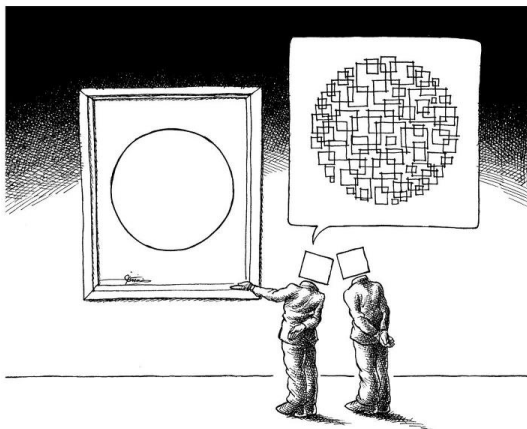
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Introduction to Interval Analysis





$$f(x, y) = 333.75y^6 + x^2(11x^2y^2 - y^6 - 121y^4 - 2) + 5.5y^8 + \frac{x}{2y}$$

Matlab	Scilab	C (double)	Maple (10 Digits)	Maple (20 digits)
-1.1806×10^{21}	-1.1806×10^{21}	1.1726039	0.1×10^{28}	-1×10^{17}

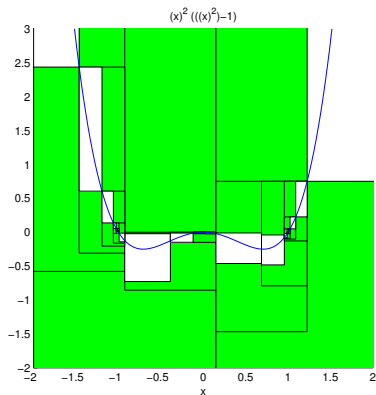
Introduction

Usages

- Finding roots of functions
- Finding extremum points
- Surfaces

Education method

Swapping teacher and student position!
Scientific negotiation!!



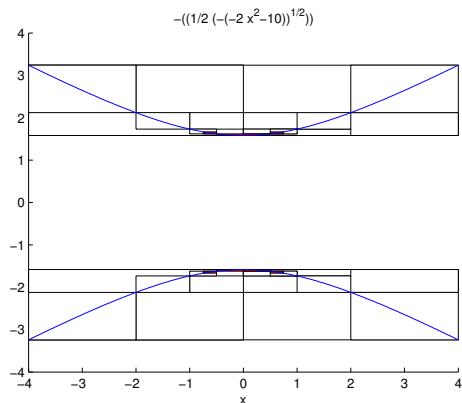
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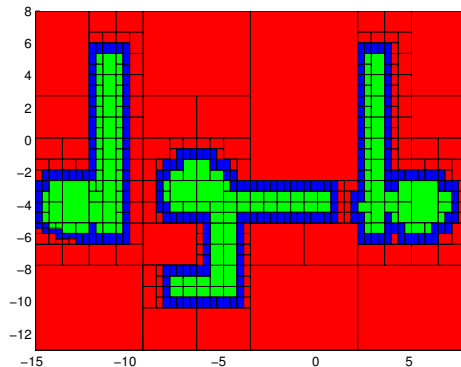
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Education Method

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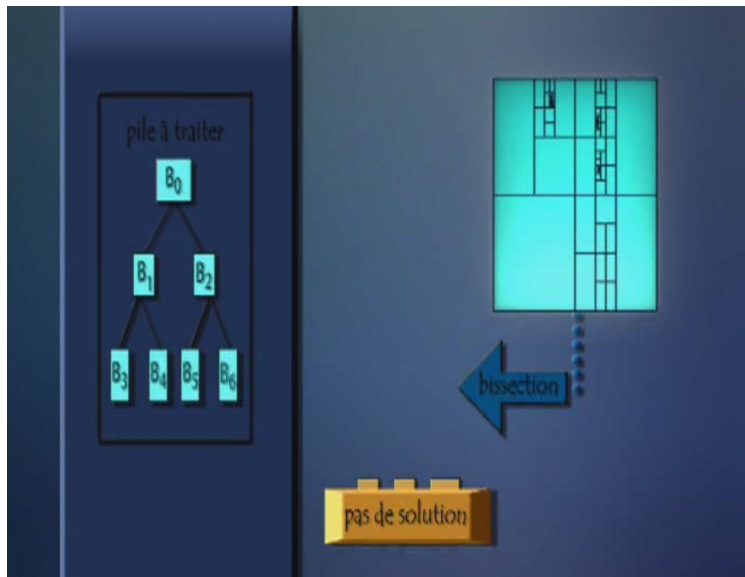
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Interval Analysis Video



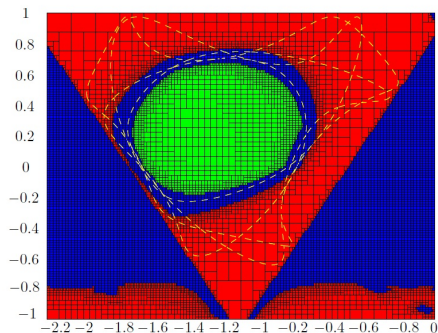
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Finding Circle

Algorithm

- Fixed center
- Unknown center \Rightarrow
Paper submitted to ICRA
2013
"The Maximal
Singularity-free Circle of
3-RPR Planar Parallel
Mechanisms Using Interval
Analysis and Geometric
Constructive Approach"

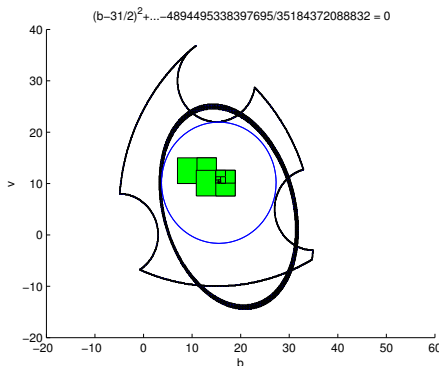


Singularity loci of 3-PRR

Finding Circle

Algorithm

- Fixed center
- Unknown center \Rightarrow
Paper submitted to ICRA
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Maximal singularity-free circle
of 3-RPR, by considering
workspace

ICRA 2013 Paper

Video submitted to ICRA 2013



University of Tehran
Faculty of New Science and Technology

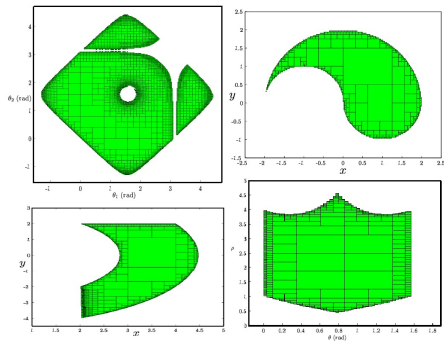
The Maximal Singularity-free Circle of 3-RPR Planar Parallel Mechanisms Using Interval Analysis

By
M. H. Farzaneh
M. T. Masouleh
B. Mashhadi

ICRoM 2013 Papers

Submitted papers

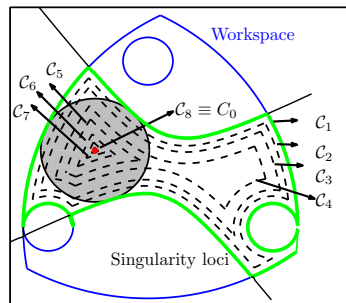
- With Mrs. Ansari, "Determining the Workspace and Joint-space of 2-DoF Serial Manipulators via Interval Analysis"
- With Mr. Mashhadi,
- With Mrs. Chae bakhsh,
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ICRoM 2013 Papers

Submitted papers

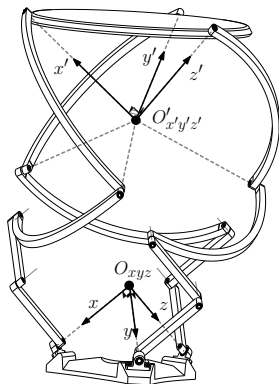
- With Mrs. Ansari,
- With Mr. Mashhadi, "The Maximal Singularity-free Circle in the Workspace of 3-RPR Planar Mechanisms Using Interval Analysis and Geometrical Approach"
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ICRoM 2013 Papers

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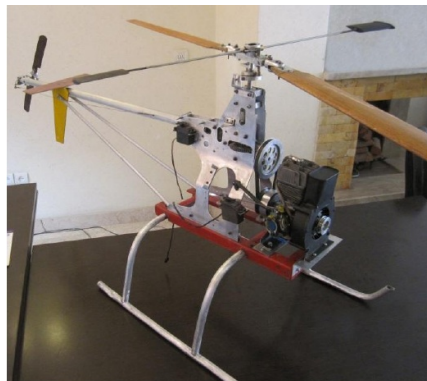
- With Mrs. Ansari,
- With Mr. Mashhadi,
- With Mrs. Chae bakhsh, "Kinematics of a Spherical Parallel Mechanism with Identical Limb Structures Using the Linear Implicitization Algorithm and Euclidean Geometry"
- With Mr. Behnam Mashhadi,



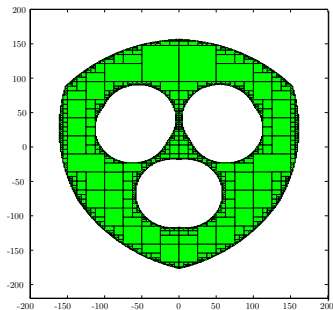
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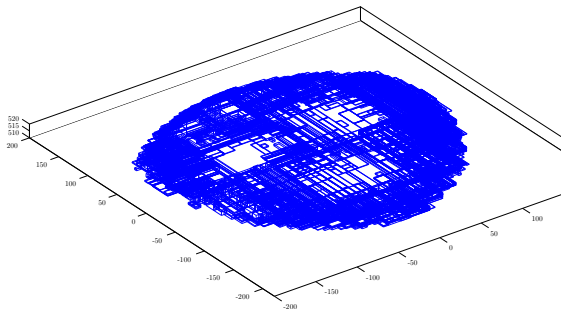
- With Mrs. Ansari,
- With Mr. Mashhadi,
- With Mrs. Chae bakhsh,
- **With Mr. Behnam Mashhadi,**
"Manufacturing of a UAV Helicopter"



3D Workspace of Gough-Stewart Platform



2D constant
orientation workspace
(COW) of
Gough-Stewart
platform, $z = 512$

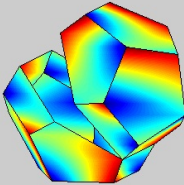


3D COW of Gough-Stewart platform,
 $z = [510, 520]$

Experiences On

Instruments

- INTLAB
- IntPakx
- ALIAS



```
x = hessianinit(xs);  
y = f(x);  
xs = xs - y.hrx\y.dx';
```

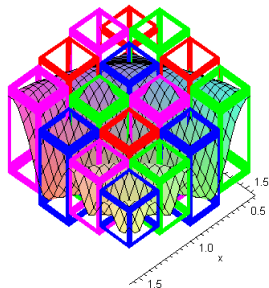
INTLAB - INTerval LABoratory (Version 6)

*The Matlab toolbox for Reliable Computing - www.ti3.tu-harburg.de/rump
Siegfried M. Rump, Institute for Reliable Computing, Hamburg University of Technology*

Experiences On

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Interval arithmetic using
MAPLE

Experiences On

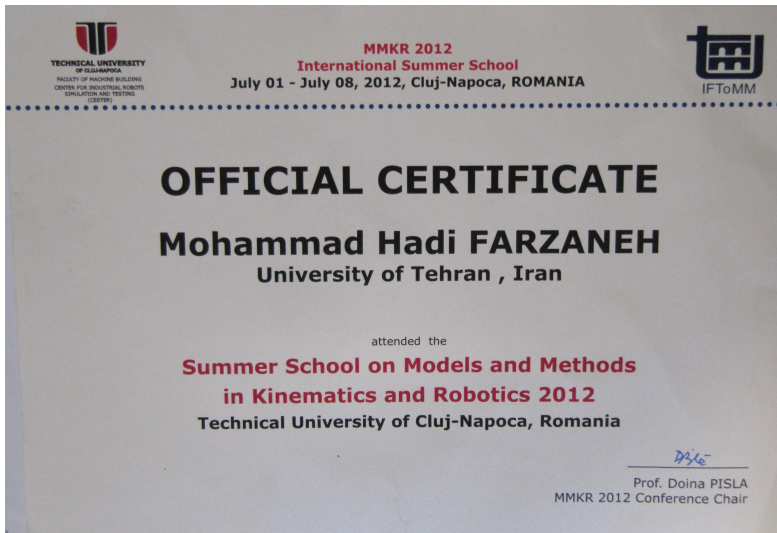
Instruments

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C++

MMKR 2012 International Summer School



MMKR 2012 International Summer School

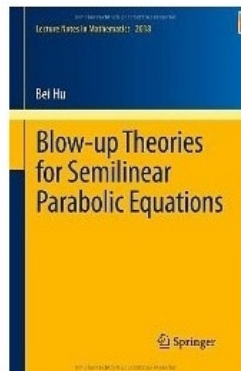


Me, Prof. J.-P. Merlet and Prof. M. L. Husty

Ongoing

Obstacles

- Find maximal singularity-free for 3-PRR
⇒ *Blows up*
- Cable-driven PMs
⇒ *Consistency*
(cooperating with Mr. Saman Esfahani)
- Grid method applicable for more complicated singularities and deals with *dexterity*



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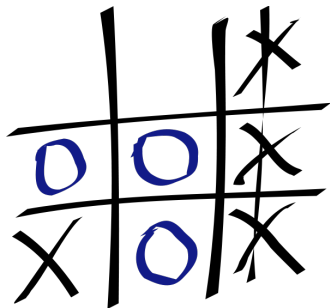
Obstacles

- Find maximal singularity-free for 3-PRR
 \Rightarrow *Blows up*

- Cable-driven PMs
 \Rightarrow *Consistency*

(cooperating with Mr. Saman Esfahani)

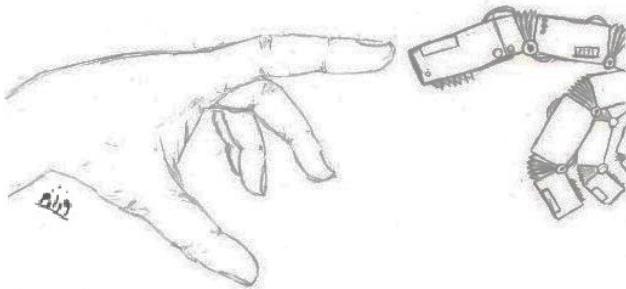
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Ongoing

Future programs

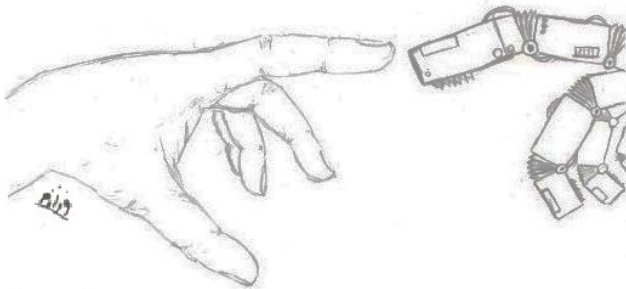
- Develop offset approach
- ALIAS
- Gough-Stewart and Cable-driven robots



Ongoing

Future programs

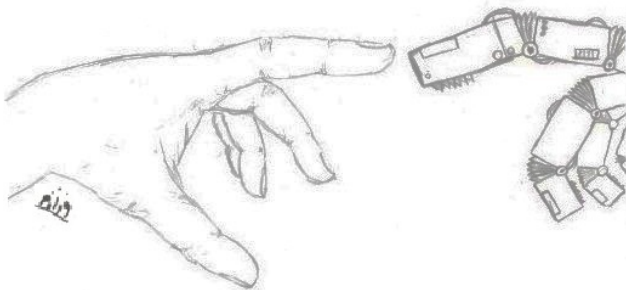
- Develop offset approach
- **ALIAS**
- Gough-Stewart and Cable-driven robots



Ongoing

Future programs

- Develop offset approach
- ALIAS
- Gough-Stewart and Cable-driven robots



Ongoing Papers

Conferences	Venue	Dead line	Conference date	Paper's subject
ISME 2013	K. N. Toosi University of Technology, Iran	20 th November 2012	5 th to 7 th May 2013	Maximum singularity-free workspace of Gough-Stewart platform
ICEE 2013	Ferdowsi University of Mashhad, Iran	1 st December 2012	14 th to 16 th May 2013	Maximum singularity-free circle (MSFC) in the workspace of Gough-Stewart platform
ISRM 2013				MSFC of 3-DoF PMs using Interval Analysis
Multi-Body Dynamics 2013	Zagreb, Croatia	30 th November 2012	1 st to 4 th July 2013	MSFC of PMs using geometrical constructive approach
AIM 2013	Wollongong, Australia	20 th January 2013	9 th to 12 th July 2013	MSFC in Wrench- Feasible Workspace (WFW) of Cable- driven robots

Ongoing Papers

Journals	Paper's subject
MMT	6-DoF Gough-Stewart platform MSFC
Robotics and Automation IEEE	On the maximal singularity-free workspace of planar PMs
	MSFC in WFW of Cable-driven robots

Schedule

Activity	1	2	3	4	5	6	7	8	9	10
Literature studies	*	*	*	*						
Optimization Approaches		*	*	*						
Interval Analysis				*	*	*				
INTLAB				*	*	*				
IntPakx					*					
ALIAS						*	*			
First paper							*			
Other Approaches								*	*	*
Second paper										*

Schedule

Activity	11	12	13	14	15	16	17	18
Other robots	*	*						
Third paper			*					
Geometry					*	*		
Fourth paper						*		
Preparing thesis						*	*	
Defending								*

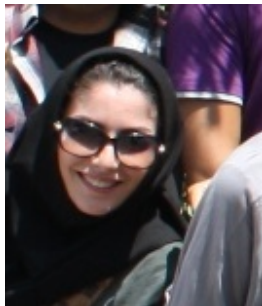
Thanks to ...

- Saman Esfehani
- Fateme Ansari
- Sarvenaz Chaei Bakhsh
- Behnam Mashhadi



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Rostam Abad

